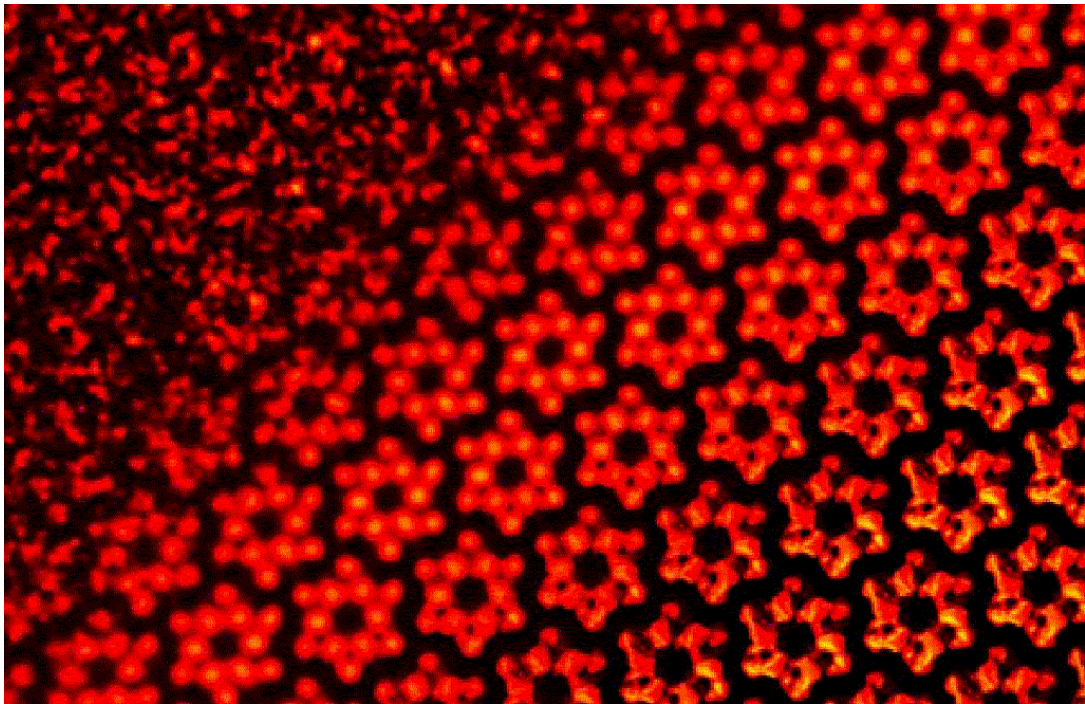


# Digital Image Processing in Natural Sciences and Medicine

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**The asymmetric membrane of the urea bladder**  
(from top left to down right : Original data; 2D reconstruction; 3D reconstruction)

Image taken from T. Walz *et al.* J Mol Biol 1995 May 19;248(5), pp. 887-900

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